



# Cambridge International AS & A Level

CANDIDATE NAME



CENTRE NUMBER

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**MATHEMATICS**

**9709/13**

Paper 1 Pure Mathematics 1

**October/November 2024**

**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages. Any blank pages are indicated.







2 Find the exact solution of the equation

$$\cos \frac{1}{6}\pi + \tan 2x + \frac{\sqrt{3}}{2} = 0 \text{ for } -\frac{1}{4}\pi < x < \frac{1}{4}\pi. \quad [2]$$

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3 (a) Find the coefficients of  $x^3$  and  $x^4$  in the expansion of  $(3 - ax)^5$ , where  $a$  is a constant. Give your answers in terms of  $a$ . [3]

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(b) Given that the coefficient of  $x^4$  in the expansion of  $(ax + 7)(3 - ax)^5$  is 240, find the positive value of  $a$ . [3]

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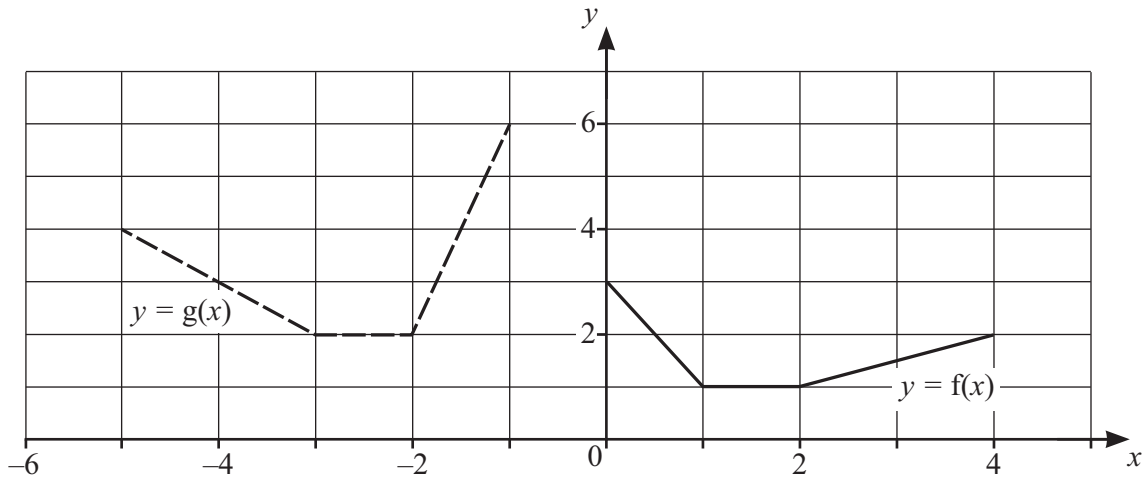
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In the diagram, the graph with equation  $y = f(x)$  is shown with solid lines and the graph with equation  $y = g(x)$  is shown with broken lines.

- (a) Describe fully a sequence of three transformations which transforms the graph of  $y = f(x)$  to the graph of  $y = g(x)$ . [6]

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- (b) Find an expression for  $g(x)$  in the form  $af(bx + c)$ , where  $a$ ,  $b$  and  $c$  are integers. [2]

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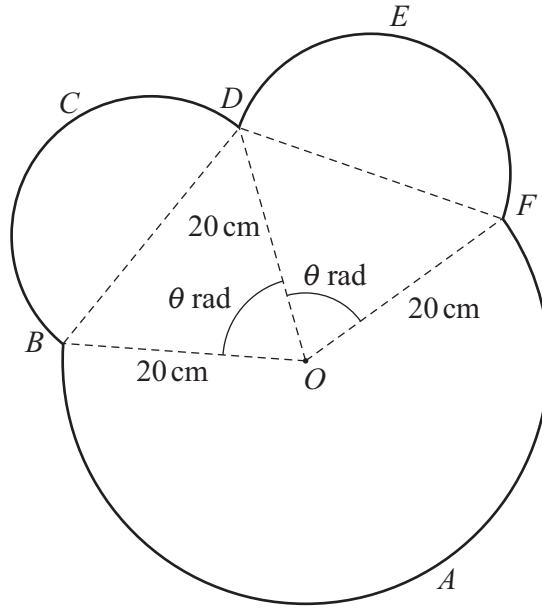
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The diagram shows a metal plate  $ABCDEF$  consisting of five parts. The parts  $BCD$  and  $DEF$  are semicircles. The part  $BAFO$  is a sector of a circle with centre  $O$  and radius 20 cm, and  $D$  lies on this circle. The parts  $OBD$  and  $ODF$  are triangles. Angles  $BOD$  and  $DOF$  are both  $\theta$  radians.

- (a) Given that  $\theta = 1.2$ , find the area of the metal plate. Give your answer correct to 3 significant figures. [5]

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Dotted lines for writing

(b) Given instead that the area of each semicircle is  $50\pi \text{ cm}^2$ , find the exact perimeter of the metal plate. [5]

Dotted lines for writing





8 (a) Express  $3x^2 - 12x + 14$  in the form  $3(x + a)^2 + b$ , where  $a$  and  $b$  are constants to be found. [2]

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The function  $f(x) = 3x^2 - 12x + 14$  is defined for  $x \geq k$ , where  $k$  is a constant.

(b) Find the least value of  $k$  for which the function  $f^{-1}$  exists. [1]

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For the rest of this question, you should assume that  $k$  has the value found in part (b).

(c) Find an expression for  $f^{-1}(x)$ . [3]

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(d) Hence or otherwise solve the equation  $ff(x) = 29$ . [3]

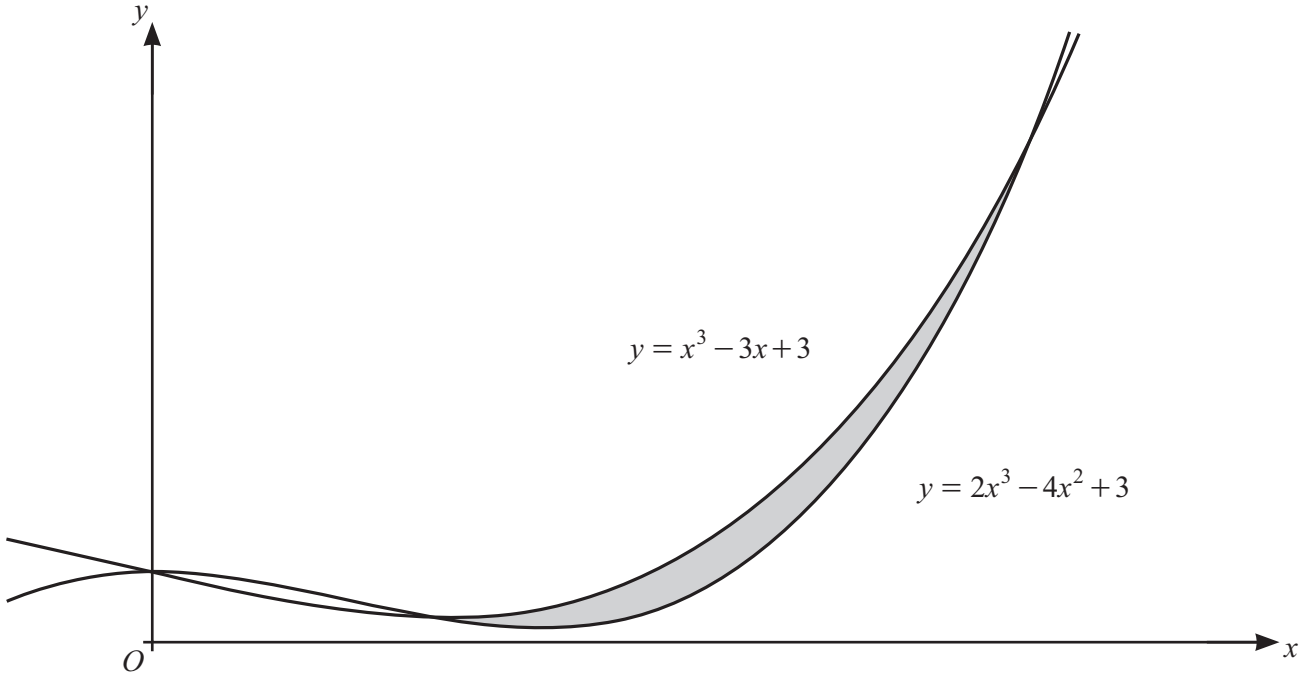
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The diagram shows the curves with equations  $y = x^3 - 3x + 3$  and  $y = 2x^3 - 4x^2 + 3$ .

- (a) Find the  $x$ -coordinates of the points of intersection of the curves. [3]

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(b) Find the area of the shaded region.

[4]

Area for student response with horizontal dotted lines.

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10 Points *A* and *B* have coordinates  $(4, 3)$  and  $(8, -5)$  respectively. A circle with radius 10 passes through the points *A* and *B*.

(a) Show that the centre of the circle lies on the line  $y = \frac{1}{2}x - 4$ . [4]

Dotted lines for writing the solution.

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(b) Find the two possible equations of the circle.

[5]

Dotted lines for writing the answer.

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11 The equation of a curve is  $y = kx^{\frac{1}{2}} - 4x^2 + 2$ , where  $k$  is a constant.

(a) Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  in terms of  $k$ . [2]

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(b) It is given that  $k = 2$ .

Find the coordinates of the stationary point and determine its nature. [4]

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**Additional page**

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